

# C.U.SHAH UNIVERSITY

## Summer Examination-2018

**Subject Name: Electromagnetics**

**Subject Code: 4TE06ELM1**

**Branch: B.Tech (Electrical)**

**Semester: 6**

**Date: 23/04/2018**

**Time: 02:30 To 05:30**

**Marks: 70**

Instructions:

- (1) Use of Programmable calculator & any other electronic instrument is prohibited.
- (2) Instructions written on main answer book are strictly to be obeyed.
- (3) Draw neat diagrams and figures (if necessary) at right places.
- (4) Assume suitable data if needed.

**Q-1**

**Attempt the following questions:**

**(14)**

- 1) A scalar has \_\_\_\_\_  
 A) Only Direction B) Only Magnitude  
 C) Both magnitude and direction D) None of the above
- 2) If  $r$  is a variable of a sphere,  $x$ ,  $y$  and  $z$  are Cartesian co-ordinates then \_\_\_\_\_  
 A)  $\vec{r} = \sqrt{x^2 + y^2 + z^2}$  B)  $\vec{r} = x^2 + y^2 + z^2$  C)  $r = x + y + z$  D) None of the above
- 3) If  $A$  and  $B$  are the vectors, then  $A \cdot B = B \cdot A$   
 A) True B) False
- 4) The equation for a line charge is given by \_\_\_\_\_  
 A)  $\int p_v dv$  B)  $\int p_L dL$  C)  $\int p_s dS$  D) None of the above
- 5) If vector  $G = 2a_x - 3a_y - a_z$ , the  $y$  component of the vector  $G$  is \_\_\_\_\_  
 A) 2 B) 3 C) -1 D) -3
- 6) For vectors  $A$  and  $B$ ,  $A \times B = -(B \times A)$ .  
 A) True B) False
- 7) The relation between Electric field intensity and force is \_\_\_\_\_  
 A)  $E = FQ$  B)  $F = \frac{F}{Q}$  C)  $E = \frac{F}{Q}$  D) None of the above



- 8) The unit of electric field intensity is \_\_\_\_\_  
 A) Coulomb/Newton B) Coulomb C) Newton D) Newton/Coulomb
- 9) If  $Q$  is the charge in a total volume  $v$ , then volume charge density  $\rho =$  \_\_\_\_  
 A)  $Q$  B)  $\frac{v}{Q}$  C)  $\frac{Q}{v}$  D)  $Q.v$
- 10) The cosine angle between  $2a_x$  and  $-a_x + 2a_y + 7a_z$  is \_\_\_\_\_  
 A)  $0^\circ$  B)  $97.8^\circ$  C)  $84.8^\circ$  D)  $45.16^\circ$
- 11) The magnitude of vector  $\vec{A} = 2 \cos \alpha \vec{a}_x + 2 \sin \alpha \vec{a}_y + 7 \vec{a}_z =$  \_\_\_\_\_  
 A) 10 B) 0 C) 3.87 D) 7.28
- 12) The unit of permittivity is given by \_\_\_\_\_  
 A) Farad/metre B) metre/Farad C) Farad D) Farad/metre<sup>2</sup>
- 13) Curl of  $H =$  \_\_\_\_\_  
 A)  $\nabla H$  B)  $\nabla \times H$  C)  $\nabla^2 H$  D)  $\nabla H^2$
- 14) For any vector  $A$  unit vector  $\vec{a}_A \cdot \vec{a}_A =$  \_\_\_\_\_  
 A) 0 B) 2 C) 5 D) 1

**Attempt any four questions from Q-2 to Q-8**

**Q-2 Attempt all questions (14)**

- (a) If  $Q_1$  and  $Q_2$  are the point charges are located at points having position vectors  $\vec{r}_1$  and  $\vec{r}_2$ , derive the equation of force  $\vec{F}_{12}$  on charge  $Q_2$  due to  $Q_1$ . **07**
- (b) If  $\mathbf{A}$  and  $\mathbf{B}$  are the vectors, explain its dot product and cross product operation. **07**

**Q-3 Attempt all questions (14)**

- (a) Derive the equation for electric field intensity  $\vec{E}$  for a finite volume charge with a uniform charge density  $\rho_v$ . **07**
- (b) Given the two points, C(-3,2,1) and D( $r=5, \theta=20^\circ, \phi=70^\circ$ ). Find **07**
- i) The spherical co-ordinates of C.
- ii) The rectangular co-ordinates of D.



- Q-4 Attempt all questions (14)**
- (a) Derive the equation  $W = -Q \int_{init}^{final} \vec{E} \cdot d\vec{L}$ , energy expended in moving a point charge **07**  
in an electric field, where  $\vec{E}$  = Electric Field,  $d\vec{L}$  = distance,  $Q$  = point charge.
- (b) Given the vectors  $\vec{M} = -10\vec{a}_x + 4\vec{a}_y - 8\vec{a}_z$  and  $\vec{N} = 8\vec{a}_x + 7\vec{a}_y - 2\vec{a}_z$ . Find **07**  
i) A unit vector in the direction of  $-\vec{M} + 2\vec{N}$ .  
ii) The magnitude of  $\vec{N} - 3\vec{M}$ .
- Q-5 Attempt all questions (14)**
- (a) Derive the equation for magnetic field intensity with the help of Bio-Savart's law. **07**
- (b) State Gauss Law. Show that electric flux  $\psi = \oint \vec{D}_s \cdot d\vec{S} = Q$ , where  $Q$  = Point **07**  
Charge  $\vec{D}_s$  = Surface Flux Density.
- Q-6 Attempt all questions (14)**
- (a) Derive the equation of Electric field intensity  $\vec{E} = \frac{Q}{4\pi \epsilon_0 R^2} \vec{a}_R$ , where  $Q$  = **07**  
Charge located at a point where  $\vec{E}$  is desired and  $\vec{a}_R$  is a unit vector in the  $\vec{R}$  direction,  $R$  is the magnitude of vector  $\vec{R}$ .
- (b) The field quantities are given by  $\vec{P} = 2\vec{a}_x - \vec{a}_z$ ,  $\vec{Q} = 2\vec{a}_x - \vec{a}_y + 2\vec{a}_z$  **07**  
 $\vec{R} = 2\vec{a}_x - 3\vec{a}_y + \vec{a}_z$   
Determine i)  $(\vec{P} + \vec{Q}) \times (\vec{P} - \vec{Q})$  ii)  $(\vec{Q} \cdot \vec{R}) \times \vec{P}$
- Q-7 Attempt all questions (14)**
- (a) State and prove the divergence theorem. **07**
- (b) A charge of  $Q_1 = 3 \times 10^{-4}$  C is located at M(1,2,3) and a charge of  $Q_2 = 10^{-4}$  C at **07**  
N(2,0,5) in a vacuum. Find the force exerted on  $Q_2$  by  $Q_1$ .
- Q-8 Attempt all questions (14)**
- (a) For a co-axial cable at high frequencies, give the equation for capacitance, **07**



conductance, inductance and resistance.

(b) Determine the following for the given vector fields.

07

i) Find divergence  $\vec{D}$  at the origin if  $\vec{D} = e^{-x} \sin y \vec{a}_x - e^{-x} \cos y \vec{a}_y + 2z \vec{a}_z$  C/m<sup>2</sup>

ii) Find divergence  $\vec{D}$  at P(2,3,-1) if  $\vec{D} = (2xyz - y^2) \vec{a}_x + (x^2z - 2xy) \vec{a}_y + x^2y \vec{a}_z$  C/m<sup>2</sup>.

